

Degree-based topological indices of polytetrafluoroethylene via M -polynomial

R. Jeyabalan [†]

G. Suthakaran ^{*}

Department of Mathematics

Alagappa University

Karaikudi

Tamil Nadu

India

S. Bala Sundar [§]

Department of Mathematics

Alagappa Chettiar Government College of Engineering and Technology

Karaikudi

Tamil Nadu

India

Abstract

The M -polynomial is important in deriving degree-based topological indices which predict different chemical and physical characteristics of the material. This article computes degree-based topological indices of polytetrafluoroethylene and provides a graphical representation of these indices and the M -polynomial.

Subject Classification (2010): 05C09, 05C92, 05C90.

Keywords: Degree-based topological index, Zagreb index, Randic index, Graph polynomial.

1. Introduction

This paper examines a simple connected graph. The degree of a vertex is the number of edges connecting it to it [3]. It is represented by d_v . The physical and chemical characteristics of substances are identified using chemical graph theory. We begin by investigating the M - polynomial [5, 7, 8], which is useful in

[†] E-mail: jeyabalanr@alagappauniversity.ac.in

^{*} E-mail: suthakarangovinthan666@gmail.com (Corresponding Author)

[§] E-mail: balasundaraccet@gmail.com

determining the degree-based topological indices of graphs. The M -polynomial of graph G is $M(G; a, b) = \sum_{\delta \leq i \leq j \leq \Delta} m_{ij}(G) a^i b^j$, where m_{ij} is the total number of edges uv , vertex u having degree i and vertex v having degree j and δ denotes minimum degree of the graph and Δ denotes maximum degree of the graph. Topological indices [2, 5] are mathematical concepts that represent the structure of molecules as graphs. The vertices of these graphs correspond to the atoms, while the edges reflect the bonds between these atoms. Topological indices serve as a valuable instrument in QSAR and QSPR investigations. We take the chemical compound polytetrafluoroethylene (PTFE) [6]. For instance, [1] explored the topological indices of H-Naphthalenic nanotubes, highlighting their utility in characterizing the structure and potential applications of these advanced materials. A significant advancement in this area was made in [4], where the authors derived a closed form for the M -polynomial of PETAA dendrimers. PTFE $[CF_2 - CF_2]_n$ has the same chemical structure as polyethylene, except that the hydrogen atoms have been completely replaced by fluorine. We determine many degree-based topological indices for PTFE utilizing the M -polynomial, show a graphical depiction of these indices, and compare the values of the degree-based topological indices for (CF_2) , $(CF_2)_2$, $(CF_2)_3$, $(CF_2)_4$, $(CF_2)_5$.

2. M -polynomial of $(CF_2)_n$

Theorem 2.1: If G be a $(CF_2)_n$ graph then M -polynomial of G is

$$M[G; a, b] = 4ab^3 + (2n - 4)ab^4 + 2a^3b^4 + (n - 3)a^4b^4, n \geq 3.$$

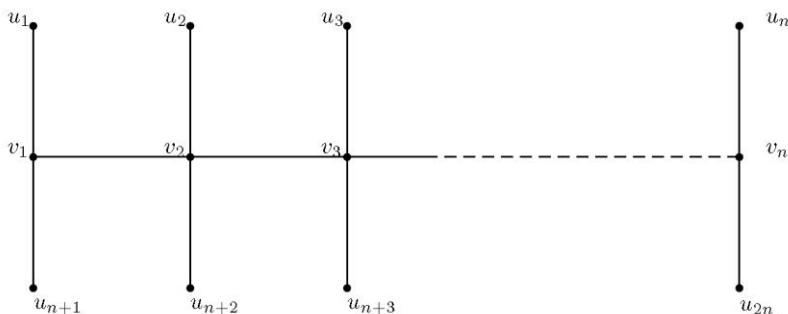
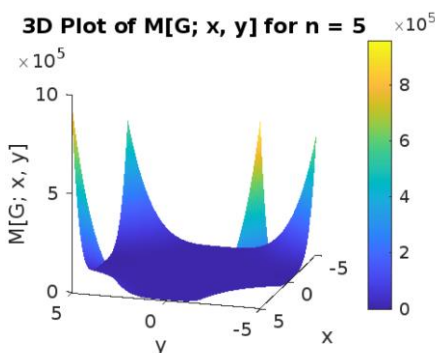


Figure 1
Polytetrafluoroethylene graph

Let $G = (CF_2)_n$ be a graph. The given figure 1 depicts the degree of the points. $d_G(v_1) = d_G(v_n) = 3$; $d_G(v_2) = d_G(v_3) = \dots = d_G(v_{n-1}) = 4$; $d_G(u_1) = d_G(u_2) = \dots = d_G(u_{n+1}) = \dots = d_G(u_{2n}) = 1$. Edge partition of G are

$$\begin{aligned} E_{1,3} &= \{uv \in G: d_u = 1, d_v = 3\} \\ E_{1,4} &= \{uv \in G: d_u = 1, d_v = 4\} \\ E_{3,4} &= \{uv \in G: d_u = 3, d_v = 4\} \\ E_{4,4} &= \{uv \in G: d_u = 4, d_v = 4\} \end{aligned}$$

$$\begin{aligned}
 m_{13} &= |E_{1,3}| = 4 \\
 m_{14} &= |E_{1,4}| = 2n - 4 \\
 m_{34} &= |E_{3,4}| = 2 \\
 m_{44} &= |E_{4,4}| = n - 3
 \end{aligned}$$



$$\begin{aligned}
 M[G; a, b] &= \sum_{\delta \leq i \leq j \leq \Delta} m_{ij}(G) a^i b^j \\
 &= \sum_{1 \leq i \leq j \leq 4} m_{ij}(G) a^i b^j \\
 &= \sum_{1 \leq i \leq 3} m_{13} a b^3 + \sum_{1 \leq i \leq 4} m_{14} a b^4 + \sum_{3 \leq i \leq 4} m_{34} a^3 b^4 + \sum_{4 \leq i \leq 4} m_{44} a^4 b^4 \\
 M[G; a, b] &= 4ab^3 + (2n - 4)ab^4 + 2a^3b^4 + (n - 3)a^4b^4, n \geq 3
 \end{aligned} \tag{1}$$

3. Topological indices of $(CF_2)_n$

We compute several topological invariants using the M -polynomial derived in the preceding section of $(CF_2)_n$. The calculation of degree-based topological indices presented in Table 1 in [7].

Theorem 3.1: If $G = (CF_2)_n$ graph and

$$M[G; a, b] = 4ab^3 + (2n - 4)ab^4 + 2a^3b^4 + (n - 3)a^4b^4, n \geq 3$$

then

- (1) $M_1[G] = 18n - 14$.
- (2) $M_2[G] = 24n - 28$.
- (3) ${}^mM_2[G] = \frac{27n+15}{48}$.
- (4) $R_\alpha[G] = 4 \cdot 3^\alpha + 4^\alpha(2n - 4) + 2 \cdot (12)^\alpha + 4^2\alpha(n - 3)4$.
- (5) $RR_\alpha[G] = \frac{4}{3^\alpha} + \frac{2n-4}{4^\alpha} + \frac{2}{12^\alpha} + \frac{n-3}{4^2\alpha}$.
- (6) $H[G] = \frac{31+147n}{140}$.
- (7) $SSD[G] = \frac{33+53n}{6}$.
- (8) $A[G] = \frac{27}{2} + \frac{4^3}{3^3}(2n - 4) + \frac{2 \cdot (12)^3}{5^3} + \frac{4^6(n-3)}{3^3}$.

- (9) $I[G] = \frac{126n-97}{35}$.
- (10) $ABC[G] = \frac{4\sqrt{2}+\sqrt{5}}{\sqrt{3}} + \frac{4\sqrt{3}n-8\sqrt{3}+\sqrt{6}n-3\sqrt{6}}{4}$.
- (11) $GA[G] = \frac{110\sqrt{3}-217+91n}{35}$.
- (12) $B_1[G] = 42n - 38$.
- (13) $B_2[G] = 78n - 102$.
- (14) $HB_1[G] = 330n - 417$.
- (15) $HB_2[G] = 1458n - 2658$.
- (16) ${}^mB_1[G] = \frac{11(n-2)}{14} + \frac{101}{36}$.
- (17) ${}^mB_2[G] = \frac{185+55n}{60}$.
- (18) $H_b[G] = \frac{69n-152}{35}$.

Proof: Here we consider

$$M[G; a, b] = h(a, b) = 4ab^3 + (2n - 4)ab^4 + 2a^3b^4 + (n - 3)a^4b^4, n \geq 3,$$

(1) The first Zagreb index

$$\begin{aligned} D_a h(a, b) &= 4ab^3 + (2n - 4)ab^4 + 6a^3b^4 + 4(n - 3)a^4b^4, \\ D_b h(a, b) &= 12ab^3 + 4(2n - 4)ab^4 + 8a^3b^4 + 4(n_3)a^4b^4, \\ (D_a + D_b)[h(a, b)] &= 16ab^3 + 5(2n - 4)ab^4 + 14a^3b^4 + 8(n - 3)a^4b^4, \\ M_1[G] = (D_a + D_b)[h(a, b)]_{a=b=1} &= 18n - 14. \end{aligned}$$

(2) The second Zagreb index

$$\begin{aligned} D_a D_b h(a, b) &= 12ab^3 + 4(2n - 4)ab^4 + 24a^3b^4 + 16(n - 3)a^4b^4, \\ M_2[G] = (D_a D_b)[h(a, b)]_{a=b=1} &= 24n - 28. \end{aligned}$$

(3) The modified second Zagreb index

$$\begin{aligned} S_b h(a, b) &= \frac{4}{3}ab^3 + \frac{(2n-4)}{4}ab^4 + \frac{2}{4}a^3b^4 + \frac{(n-3)}{4}a^4b^4, \\ S_a S_b h(a, b) &= \frac{4}{3}ab^3 + \frac{2n-4}{4}ab^4 + \frac{2}{12}a^3b^4 + \frac{n-3}{16}a^4b^4, \\ {}^mM_2[G] = (S_a S_b)[h(a, b)]_{a=b=1} &= \frac{27n+15}{48}. \end{aligned}$$

(4) The general Randic index

$$\begin{aligned} D_b^\alpha h(a, b) &= 4 \cdot 3^\alpha ab^3 + a^\alpha (2n - 4)ab^4 + 2 \cdot 4^\alpha a^3b^4 + 4^\alpha (n - 3)a^4b^4, \\ D_a^\alpha D_b^\alpha h(a, b) &= 4 \cdot 3^\alpha ab^3 + 4^\alpha (2n - 4)ab^4 + 2 \cdot 12^\alpha a^3b^4 + 4^{2\alpha} (n - 3)a^4b^4, \\ {}^mM_2[G] = (D_a^\alpha D_b^\alpha)h(a, b)_{a=b=1} &= 4 \cdot 3^\alpha + 4^\alpha (2n - 4) + 2 \cdot 12^\alpha + 4^{2\alpha} (n - 3). \end{aligned}$$

(5) The Inverse Randic index

$$\begin{aligned}
S_b^\alpha h(a, b) &= \frac{4}{3^\alpha} ab^3 + \frac{2n-4}{4^\alpha} ab^4 + \frac{2}{4^\alpha} a^3 b^4 + \frac{n-3}{4^\alpha} a^4 b^4, \\
S_a^\alpha S_b^\alpha h(a, b) &= \frac{4}{3^\alpha} ab^3 + \frac{2n-4}{4^\alpha} ab^4 + \frac{2}{12^\alpha} a^3 b^4 + \frac{n-3}{4^{2\alpha}} a^4 b^4, \\
RR_\alpha[G] &= (S_a^\alpha S_b^\alpha)[h(a, b)]_{a=b=1} = \frac{4}{3^\alpha} + \frac{2n-4}{4^\alpha} + \frac{2}{12^\alpha} + \frac{n-3}{4^{2\alpha}}.
\end{aligned}$$

(6) The harmonic index

$$\begin{aligned}
Jh(a, b) &= 4a^4 + (2n-4)a^5 + 2a^7 + (n-3)a^8, \\
S_a Jh(a, b) &= a^4 + \frac{2n-4}{5} a^5 + \frac{2}{7} a^7 + \frac{n-3}{8} a^8, \\
2S_a Jh(a, b) &= 2a^4 + \frac{2(2n-4)}{5} a^5 + \frac{4}{7} a^7 + \frac{n-3}{4} a^8, \\
H[G] &= 2S_a J[h(a, b)] = \frac{31+147n}{140}.
\end{aligned}$$

(7) The symmetric division index

$$\begin{aligned}
D_a S_b h(a, b) &= \frac{4}{3} ab^3 + \frac{2n-4}{4} ab^4 + \frac{3}{2} a^3 b^4 + (n-3)a^4 b^4, \\
S_a D_b h(a, b) &= 12ab^3 + 4(2n-4)ab^4 + \frac{8}{3} a^3 b^4 + (n-3)a^4 b^4, \\
SSD[G] &= (D_a S_b + S_a D_b)[h(a, b)]_{a=b=1} = \frac{33+53n}{6}.
\end{aligned}$$

(8) The augmented index

$$\begin{aligned}
D_b^3 h(a, b) &= 4 \cdot 3^3 ab^3 + 4^3 (2n-4)ab^4 + 2 \cdot 4^3 a^3 b^4 + 4^3 (n-3)a^4 b^4, \\
D_a^3 D_b^3 h(a, b) &= 4 \cdot 3^3 ab^3 + 4^3 (2n-4)ab^4 + 2 \cdot 12^3 a^3 b^4 + 4^6 a^4 b^4, \\
JD_a^3 D_b^3 h(a, b) &= 4 \cdot 3^3 a^4 + 4^3 (2n-4)a^5 + 2 \cdot 12^3 a^7 + 4^6 a^8, \\
Q_{(-2)} JD_a^3 D_b^3 h(a, b) &= 4 \cdot 3^3 a^2 + 4^3 (2n-4)a^3 + 2 \cdot 12^3 a^5 + 4^6 a^6, \\
S_a^3 Q_{(-2)} JD_a^3 D_b^3 h(a, b) &= \frac{4 \cdot 3^3}{2^3} a^2 + \frac{4^3 (2n-4)}{3^3} a^3 + \frac{2 \cdot 12^3}{5^3} a^5 + \frac{4^6 (n-3)}{6^3} a^6, \\
A[G] &= S_a^3 Q_{(-2)} JD_a^3 D_b^3 [h(a, b)]_{a=b=1} = \frac{4 \cdot 3^3}{2^3} + \frac{4^3}{3^3} (2n-4) + \frac{2 \cdot 12^3}{5^3} + \frac{4^6}{6^3}.
\end{aligned}$$

(9) The inverse sum index

$$\begin{aligned}
(JD_a D_b)h(a, b) &= 12a^4 + 4(2n-4)a^5 + 24a^7 + 16(n-3)a^8, \\
(S_a J D_a D_b)h(a, b) &= 3a^4 + \frac{4(2n-4)}{5} a^5 + \frac{24}{7} a^7 + 2(n-3)a^8, \\
I[G] &= S_a J D_a D_b [h(a, b)] = \frac{126n-97}{35}.
\end{aligned}$$

(10) The atom-bond connectivity index

$$\begin{aligned}
S_a^{1/2} S_b^{1/2} h(a, b) &= \frac{4}{\sqrt{3}} ab^3 + (n-2)ab^4 + \frac{1}{\sqrt{3}} a^3 b^4 + \frac{n-3}{4} a^4 b^4, \\
JS_a^{1/2} S_b^{1/2} h(a, b) &= \frac{4}{\sqrt{3}} a^4 + (n-2)a^5 + \frac{1}{\sqrt{3}} a^7 + \frac{n-3}{4} a^8,
\end{aligned}$$

$$\begin{aligned}
Q(-2)JS_a^{1/2}S_b^{1/2}h(a,b) &= \frac{4}{\sqrt{3}}a^2 + (n-2)a^3 + \frac{1}{\sqrt{3}}a^5 + \frac{n-3}{4}a^6, \\
D_a^{1/2}Q(-2)JS_a^{1/2}S_b^{1/2}h(a,b) &= \frac{4\sqrt{2}}{\sqrt{3}}a^2 + \sqrt{3}(n-2)a^3 + \frac{\sqrt{5}}{\sqrt{3}}a^5 + \frac{\sqrt{6}(n-3)}{4}a^6, \\
ABC[G] &= D_a^{1/2}Q(-2)JS_a^{1/2}S_b^{1/2}[h(a,b)]_{a=b=1}, \\
&= \frac{4\sqrt{2}+\sqrt{5}}{\sqrt{3}} + \frac{4\sqrt{3}n-8\sqrt{3}+\sqrt{6}n-3\sqrt{6}}{4}.
\end{aligned}$$

(11) The geometric arithmetic index

$$\begin{aligned}
D_a^{1/2}D_b^{1/2}h(a,b) &= 4\sqrt{3}ab^3 + 2(2n-4)ab^4 + 4\sqrt{3}a^3b^4 + 4(n-3)a^4b^4, \\
JD_a^{1/2}D_b^{1/2}h(a,b) &= 4\sqrt{3}a^4 + 2(2n-4)a^5 + 4\sqrt{3}a^7 + 4(n-3)a^8, \\
S_aJD_a^{1/2}D_b^{1/2}h(a,b) &= \sqrt{3}a^4 + \frac{2}{5}(2n-4)a^5 + \frac{4\sqrt{3}}{7}a^7 + \frac{(n-3)}{2}a^8, \\
2S_aJD_a^{1/2}D_b^{1/2}h(a,b) &= 2\sqrt{3}a^4 + \frac{4}{5}(2n-4)a^5 + \frac{8\sqrt{3}}{7}a^7 + (n-3)a^8, \\
GA[G] &= 2S_aJD_a^{1/2}D_b^{1/2}[h(a,b)]_{a=b=1}, \\
&= \frac{110\sqrt{3}-217+91n}{35}.
\end{aligned}$$

(12) The first K Banhatti index

$$\begin{aligned}
(D_a + D_b)h(a,b) &= 18n - 14, \\
2D_aQ(-2)Jh(a,b) &= 16a^2 + 6(2n-4)a^3 + 20a^5 + 12(n-3)a^6, \\
B_1[G] &= 2D_aQ(-2)Jh(a,b)_{a=1}, \\
&= 42n - 38.
\end{aligned}$$

(13) The second K Banhatti index

$$\begin{aligned}
J(D_a + D_b)h(a,b) &= 16a^4 + 5(2n-4)a^5 + 14a^7 + 8(n-3)a^8, \\
D_aQ(-2)J(D_a + D_b)h(a,b) &= 32a^2 + 15(2n-4)a^3 + 70a^5 + 48(n-3)a^6, \\
B_2[G] &= D_aQ(-2)J(D_a + D_b)[h(a,b)]_{a=1}, \\
&= 78n - 102.
\end{aligned}$$

(14) The first K hyper Banhatti index

$$\begin{aligned}
(D_a^2 + D_b^2)h(a,b) &= 40ab^3 + 17(2n-4)ab^4 + 50a^3b^4 + 32(n-3)a^4b^4, \\
2D_a^2Q(-2)Jh(a,b) &= 32a^2 + 18(2n-4)a^3 + 100a^5 + 72(n-3)a^6, \\
2D_aQ(-2)J(D_a + D_b)h(a,b) &= 64a^2 + 30(2n-4)a^3 + 140a^5 + 96(n-3)a^6, \\
HB_1[G] &= (D_a^2 + D_b^2 + 2D_a^2Q(-2)J + 2D_aQ(-2)J(D_a + D_b))[h(a,b)], \\
&= 330n - 417.
\end{aligned}$$

(15) The second K hyper Banhatti index

$$J(D_a^2 + D_b^2)h(a,b) = 40a^4 + 17(2n-4)a^5 + 50a^7 + 32(n-3)a^8,$$

$$\begin{aligned}
Q(-2)J(D_a^2 + D_b^2)h(a, b) &= 40a^2 + 17(2n-4)a^3 + 50a^5 + 32(n-3)a^6, \\
D_a^2 Q(-2)J(D_a^2 + D_b^2)h(a, b) &= 160a^2 + 153(2n-4)a^3 + 1250a^5 + 1152(n-3)a^6, \\
HB_2[G] &= D_a^2 Q(-2)J(D_a^2 + D_b^2)[h(a, b)]_{a=1}, \\
&= 1458n - 2658.
\end{aligned}$$

(16) Modified first K Banhatti index

$$\begin{aligned}
L_a h(a, b) &= 4a^2 b^3 + (2n-4)a^2 b^4 + 2a^6 b^4 + (n-3)a^8 b^4, \\
L_b h(a, b) &= 4ab^6 + (2n-4)ab^8 + 2a^3 b^8 + (n-3)a^4 b^8, \\
J(L_a + L_b)h(a, b) &= 4a^5 + (2n-4)a^6 + 2a^{10} + 4a^7 + (2n-4)a^9 + 2a^{11} + 2(n-3)a^{12}, \\
Q(-2)J(L_a + L_b)h(a, b) &= 4a^3 + (2n-4)a^4 + 4a^5 + (2n-4)a^7 + 2a^8 + 2a^9 \\
&\quad + 2(n-3)a^{10}, \\
S_a Q(-2)J(L_a + L_b)h(a, b) &= \frac{4}{3}a^3 + \frac{2n-4}{4}a^4 + \frac{4}{5}a^5 + \frac{2n-4}{7}a^7 + \frac{1}{8}a^8 \\
&\quad + \frac{2}{9}a^9 + \frac{n-3}{5}a^{10}, \\
{}^m B_1[G] &= S_a Q(-2)J(L_a + L_b)[h(a, b)]_{a=1}, \\
&= \frac{11(n-2)}{14} + \frac{101}{36}.
\end{aligned}$$

(17) Modified second K Banhatti index

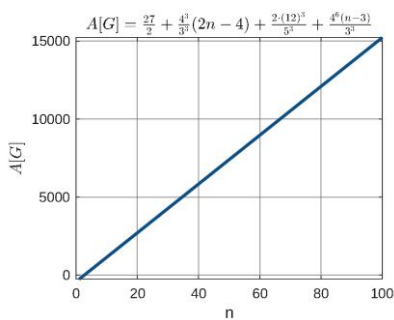
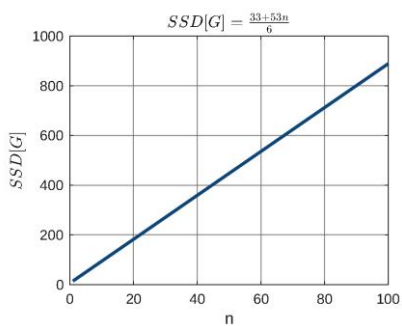
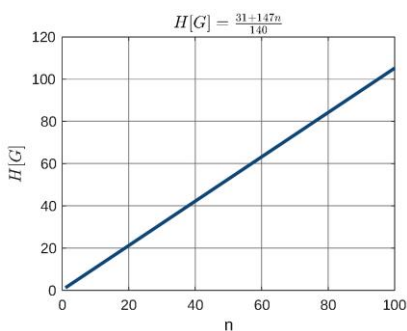
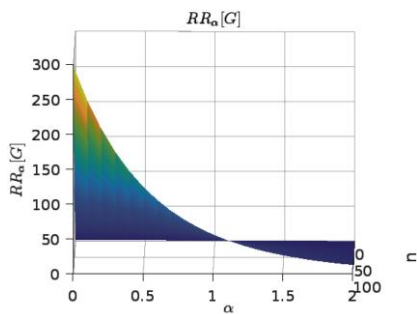
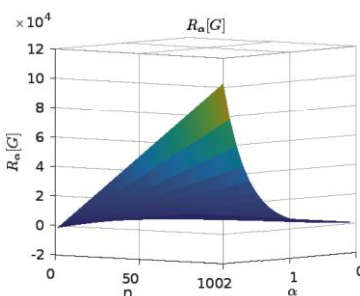
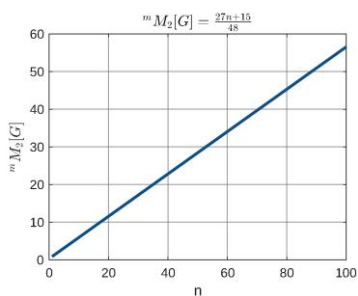
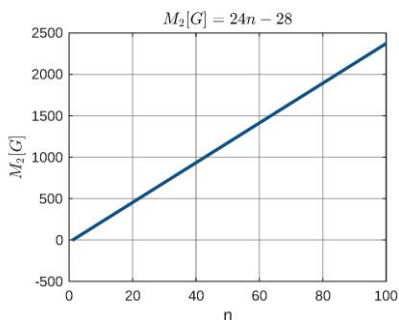
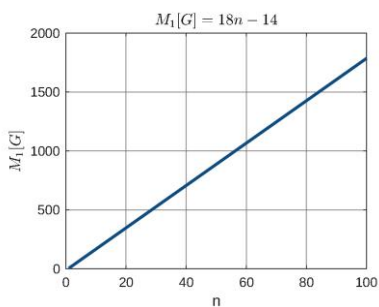
$$\begin{aligned}
(S_a + S_b)h(a, b) &= \frac{16}{3}ab^3 + \frac{10(n-2)}{4}ab^4 + \frac{7}{6}a^3b^4 + \frac{n-3}{2}a^4b^4, \\
J(S_a + S_b)h(a, b) &= \frac{16}{3}a^4 + \frac{10(n-2)}{4}a^5 + \frac{7}{6}a^7 + \frac{n-3}{2}a^8, \\
S_a Q(-2)J(S_a + S_b)h(a, b) &= \frac{8}{3}a^2 + \frac{5(n-2)}{6}a^3 + \frac{7}{30}a^5 + \frac{n-3}{12}, \\
{}^m B_2[G] &= S_a Q(-2)J(S_a + S_b)[h(a, b)]_{a=1}, \\
&= \frac{185+55n}{60}.
\end{aligned}$$

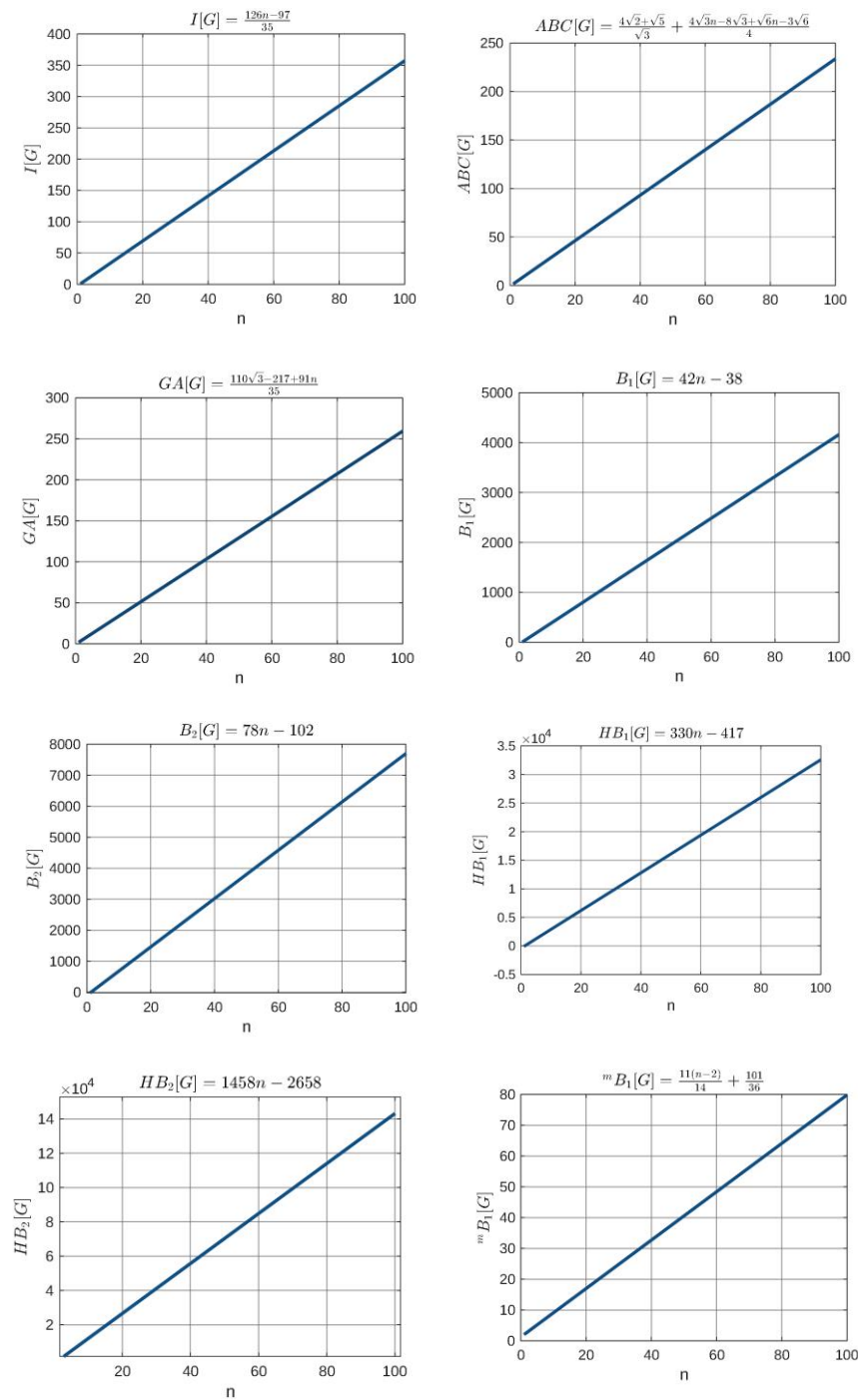
(18) Harmonic K Banhatti index

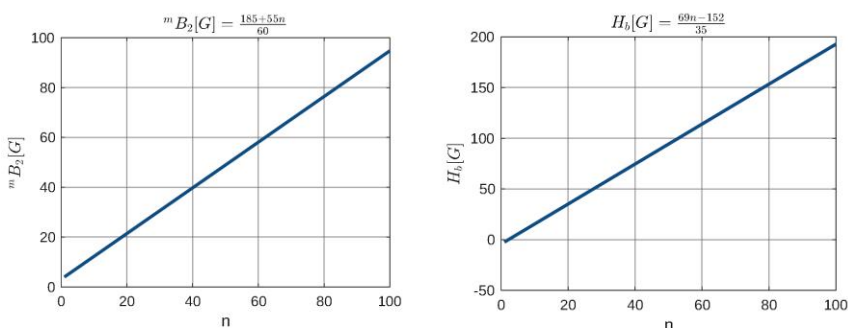
$$\begin{aligned}
2S_a Q(-2)J(L_a + L_b)h(a, b) &= \frac{8}{3}a^3 + (n-2)a^4 + \frac{8}{5}a^5 + \frac{4(n-2)}{7}a^7 + \\
&\quad \frac{1}{8}a^8 + \frac{4}{9}a^9 + \frac{2(n-3)}{5}a^{10}, \\
H_b[G] &= 2S_a Q(-2)J(L_a + L_b)[h(a, b)]_{a=1}, \\
&= \frac{69n-152}{35}.
\end{aligned}$$

4. Comparison of Topological indices

We calculate the topological index values for CF_2 , $(CF_2)_2$, $(CF_2)_3$, $(CF_2)_4$, $(CF_2)_5$ in this section.





**Table 1**

Values for the topological indices of (CF_2) , $(CF_2)_2$, $(CF_2)_3$, $(CF_2)_4$, $(CF_2)_5$.

Topological indices	CF_2	$(CF_2)_2$	$(CF_2)_3$	$(CF_2)_4$	$(CF_2)_5$
$M_1[G]$	4	22	40	58	76
$M_2[G]$	-4	20	44	68	92
$^mM_2[G]$	0.875	1.437	2	2.562	3.125
$H[G]$	1.271	2.321	3.371	4.421	5.471
$SSD[G]$	14.33	23.16	32	40.80	49.66
$I[G]$	0.828	4.428	8.028	11.628	15.228
$ABC[G]$	1.6	3.9	6.288	8.632	10.955
$GA[G]$	1.843	4.443	7.04	9.64	12.24
$B_1[G]$	4	6	88	138	172
$B_2[G]$	-24	54	132	210	288
$HB_1[G]$	-87	243	573	903	1233
$HB_2[G]$	-1200	258	1716	3174	4672
$^mB_1[G]$	2.020	2.805	3.590	4.376	4.714
$^mB_2[G]$	4	4.92	5.83	6.75	7.67
$H_b[G]$	-2.37	-0.4	1.57	3.54	5.54

5. Conclusion

The M-polynomial and topological indices of polytetrafluoroethylene (PTFE) were derived, and the degree-based topological indices for (CF_2) , $(CF_2)_2$, $(CF_2)_3$, $(CF_2)_4$, $(CF_2)_5$ were computed. The topological indices indicate the characteristics of polytetrafluoroethylene.

Acknowledgements

The article has been written with the joint financial support of RUSA-Phase 2.0 grant sanctioned vide letter No. F 24-51/2014-U, Policy (TN Multi-Gen), Dept. of Edn. Govt. of India, Dt. 09.10.2018, UGC-SAP (DRS-I) vide letter No.F.510/8/DRS-I/2016(SAP-I) Dt. 23.08.2016, DST-PURSE 2nd Phase programme vide letter No. SR/PURSE Phase 2/38 (G) Dt. 21.02.2017 and DST (FST - level I) 657876570 vide letter No.SR/FIST/MS-I/2018/17 Dt. 20.12.2018.

References

- [1] F. Afzal, S. Hussain, D. Afzal, and S. Razaq, "Some new degree-based topological indices via M-polynomial," *J. Inf. Optim. Sci.*, vol. 41, no. 4, pp. 1061-1076 (2020), doi: 10.1080/02522667.2020.1744307.
- [2] A. T. Balaban and J. Devillers, *Topological indices and related descriptors in QSAR and QSPR*, CRC Press (2018).
- [3] J. A. Bondy and U. S. R. Murty, *Graph Theory*, Springer, New York (2008).
- [4] M. Cancan, S. Ediz, H. Mutee-Ur-Rehman, and D. Afzal, "M-polynomial and topological indices Poly (EThyleneAmidoAmine) dendrimers," *J. Inf. Optim. Sci.*, vol. 41, no. 4, pp. 1117-1131 (2020), doi: 10.1080/02522667.2020.1745383.
- [5] E. Deutsch and S. Klavar, "M-polynomial and degree-based topological indices," *Iranian J. Math. Chem.*, vol. 6, no. 2, pp. 93-102 (2015), doi: 10.22052/ijmc.2015.10106.
- [6] S. Ebnesajjad, *Expanded PTFE Applications Handbook: Technology, Manufacturing and Applications*, Elsevier (2016).
- [7] A. J. M. Khalaf, S. Hussain, D. Afzal, F. Afzal, and A. Maqbool, "M-polynomial and topological indices of book graph," *J. Discrete Math. Sci. Cryptogr.*, vol. 23, no. 6, pp. 1217-1237 (2020), doi: 10.1080/09720529.2020.1809115.
- [8] S. Mondal, M. Imran, N. De, and A. Pal, "Neighborhood M-polynomial of titanium compounds," *Arabian J. Chem.*, vol. 14, no. 103244 (2021), doi: 10.1016/j.arabjc.2021.103244.

Received May, 2024